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ERRATA

MATHEMATICS FOR THE INTERNATIONAL STUDENT MATHEMATICS HL (Option): Discrete Mathematics

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The following erratum was made on 10/Jun/2016

page 207 ANSWERS EXERCISE 2A Question 10, should read:

The following erratum was made on 25/May/2016

page 52 **SECTION D Example 23,** should read:

Example 23

Prove that $\sqrt{2}$ is irrational.

Proof: (By contradiction)

Suppose that $\sqrt{2}$ is rational.

$$\therefore \quad \sqrt{2} = \frac{p}{q} \quad \text{where} \quad p, \, q \in \mathbb{Z}^+, \ \, \gcd(p, \, q) = 1$$

Since gcd(p, q) = 1, there exist $r, s \in \mathbb{Z}$ such that rp + sq = 1

Hence,
$$\sqrt{2} = \sqrt{2}(rp + sq) = (\sqrt{2}p)r + (\sqrt{2}q)s$$

$$\therefore \quad \sqrt{2} = (\sqrt{2}\sqrt{2}q)r + (\sqrt{2}\,\frac{p}{\sqrt{2}})s \qquad \text{ \{using } \ \sqrt{2} = \frac{p}{q}\}$$

$$\therefore \ \sqrt{2} = 2qr + ps$$

$$\therefore$$
 $\sqrt{2}$ is an integer

 $\{\text{since }p,\,q\in\mathbb{Z}^+,\ \text{and}\ r,\,s\in\mathbb{Z}\}$

This is a contradiction, so $\sqrt{2}$ must be irrational.

We saw a different proof for the irrationality of $\sqrt{2}$ earlier.

